Integration strategy under demand uncertainty
A real option approach

CARLOS PINHO, RUI FERNANDES & JOAQUIM BORGES GOUVEIA

ABSTRACT: Global outsourcing has emerged as one of the major approaches to gaining a worldwide competitive edge for many industries. This paper investigates companies’ flexibility, in very uncertain markets, in adapting their internal capacity so as to become an alternative to outsourcing. The capacity to be installed and the related resources allocation will be determinant for timing the change. We intend to quantify the impact of anticipating a capacity expansion, treated as a partially irreversible investment. Unlike earlier studies, it provides analytical research on the probability of switching from outsourcing to an integration option, and the expected timing of the switch under two regimes: full and partial insourcing.

Key words: Operations Integration, Outsourcing, Real Options, Uncertainty

TÍTULO: Estratégia de integração com incerteza da procura: Abordagem das opções reais

RESUMO: O outsourcing global emergiu como uma das principais abordagens em muitas indústrias, tendo em vista ganhar vantagem competitiva. Neste trabalho analisa-se a flexibilidade das empresas em adaptar a sua capacidade interna de forma a se tornar uma alternativa ao outsourcing em mercados com elevada incerteza. A capacidade a ser
INTRODUCTION

The switch strategy between outsourcing and insourcing is time-consuming due to the increased sophistication of equipment and the training time required for production workers. One way to deal with this trend is to anticipate integration, for which a trigger moment is key. Earlier studies typically focused on the value generated from the flexibility associated with the option to outsource. This paper provides a model for the likelihood of exercising the option to insource, namely, the probability of switching from outsourcing and the expected time to making such a switch.

The model presents a simple, and yet unique, analytical framework for investigating questions related to insourcing. It also identifies a series of insights related to the value associated with the flexibilities (full or partial insourcing), the likelihood of insourcing, and the expected timing of the switch in strategy.

The use of the real options methodology is based on switching costs between outsourcing and required investments in insourcing that can also be applied for an inverse strategy. For this purpose, we consider the cost to switch from insourcing to outsourcing as the diseconomies of scale related with actual use of internal capacity.

In this study we emphasize two questions: (i) How can we value a decision on integration, using outsourcing as an alternative? (ii) How can we find the trigger moment to apply for that capacity increase decision?

We will explore two hypotheses:
• Regime 1: full insourcing
• Regime 2: partial insourcing
The remainder of the paper is organized as follows. The next section reviews the related literature. Then the third section presents the model and derivations under full and partial insourcing regimes. The fourth section presents the case study and the main results. The last section concludes and suggests future research.

LITERATURE REVIEW

The literature review will be presented in three parts considering: the use of real options in operational decisions and capacity options, managerial implications of outsourcing and insourcing advantages.

The first part deals with the use of real and capacity options in operational decision-making. Birge (2000) and Dixit and Pindyk (1994) provided good examples of how option pricing can incorporate financial risk attitudes into operational decision-making. A relevant stream of research deals with capacity decisions under demand uncertainty. In these papers, the firm’s decision to invest in a capacity increase resembles the insourcing decision in our model. Van Mieghem (1999) developed outsourcing conditions using price only and incomplete contracts for subcontracting decisions. Van Mieghem and Rudi (2002) established a news-vendor network in a single-period model, and under identically and independently distributed market demands. Van Mieghem (2003) provided a comprehensive summary of various capacity investment models. Tan (2004) determined the firm’s optimal production and subcontracting decisions that ensure the long-term availability of capacity at the facility of the subcontractor. Tomlin and Wang (2005) compared the values from several forms of chain design. In the same line, Lu and Van Mieghem (2009) investigated the firm’s network design from centralization to decentralization and mentioned the influence of fixed costs in centralizing operations in a single facility. Our emphasis provides insight into the probabilistic nature of insourcing and outsourcing in a continuous-time model.

The second part is related with managerial implications of outsourcing as an alternative to achieving competitive advantages (see Gilley and Rasheed, 2000). Only few authors have been investigating the impact of such an alternative on the firm’s economic performance (e.g. Fixler and Siegel, 1999; Jiang et al. (2006); Kurz, 2004; Mol et al., 2005; Ten and Wolff, 2001). Of the few stated studies, we can find some management impacts structured in different classes, for instance, Quinn and Hilmer (1994) made an overview on strategic implications; Lever (1997) placed special attention on financial and human resources implications; Rabinovich et al. (1999), Andersson and Norrman (2002), concentrated on logistic functions; Momme (2002) studied the impact in the control dimension by focusing on the core activities.
Reitzig and Wagner (2010) concluded that a firm increases performance by conducting downstream activities and, Sharda and Chatterjee (2011) defended that there are similarities and differences between outsourcing firms and their performance, due to combinations of work designs, strategy and market relations. Other studies have focused on the benefits and risks of an outsourcing decision (e.g. Jiang et al. (2007); Schniederjans and Zuckweiler, 2004). Briefly we can identify three different approaches: the focus on strategic core competences (e.g. Quinn and Hilmer, 1994; Prahalad and Hamel, 1990; Sanders, et al., 2007), cost impacts (e.g. Holcomb and Hitt, 2007) and the resource management approach (e.g. McIvor, 2009). Despite these past considerations, we are also interested in the papers that study outsourcing from the operational planning level even though, based on scale economies reasoning, some companies outsource despite no cost advantage (Cachon and Harker, 2002). Specifically, our study will concentrate on outsourcing decisions when a company faces a potential capacity expansion, namely the decision whether to build or expand own production capacity. Mathematical models have been developed to evaluate the benefits of expanding capacity and outsourcing (e.g. Mieghem, 1999; Tsai and Lai, 2007). Kouvelis and Milner (2002) show that greater market demand uncertainty increases the reliance on outsourcing, whereas greater supply uncertainty increases the need for vertical integration. The option to outsource in production planning models results in production smoothing (Kamien and Li, 1990) and with different amounts of safety stocks needed in a supply chain (Malek et al., 2005). The effect of outsourcing on company productivity is dependent on the nature of the outsourced inputs (services or materials) (Gorg and Hanley, 2005).

The literature summarizes a number of advantages and disadvantages of outsourcing, although empirical data are still rare (Beaumont and Sohal, 2004; Bengtsson and Haartman, 2005; Gilley and Rasheed, 2000). Manufacturing cost reductions, lower investment and consequently fewer fixed capital costs are the most prominent of the disclosed advantages of outsourcing as they improve short term profitability. The modern theory of the firm has made considerable progress in explaining the determinants of vertical integration, assuming that the level of vertical integration results from independent transactional choices (Macher and Richman, 2008; Masten and Saussier, 2002; Novak and Stern, 2009; Whinston, 2003). Some approaches were made considering the uncertainty effect in an outsourcing option, based on production cost and degree of product differentiation (e.g. Hamada, 2010), market uncertainty and the optimal proportion of outsourcing (Álvarez and Stenbacka, 2007; Li and Wang, 2010), competition and foreign exchange uncertainty (Liu and Nagurney, 2011), and demand uncertainty from the outsourcing side (Boulaksil et al., 2011).
One prominent perspective to explain vertical integration is that of transaction cost economics. Its focus is on market failure and it captures ways to reduce risks by integrating economic activities under a coordinated management. According to transaction cost economics, the question of whether an activity should be integrated or not depends on the specificity of the investment, the frequency and the costs of interaction between firm and the supplier, the amount of uncertainty and an eventual opportunity for the supplier (Williamson, 2008), due for example to economies of scale (Argyres, 1996). Recently, Ciliberto and Panzar (2011) analyzed the relation between outsourcing decisions on downstream activities and the fixed costs at the upstream stages of a supply chain. Another perspective is the resource-based view of the firm focusing on internal capabilities as the main criteria for outsourcing decisions (e.g. Conner and Prahalad, 1996; Zander and Kogut, 1995). In the resource-based view of the firm, the management team devotes specific attention to the development of the organization’s internal resources and capabilities as a key competitive advantage (Teece et al., 1997). Olausson and Magnusson (2011) devoted special attention to human resources requirements and coordination; Zirpoli and Becker (2011) addressed the problem of outsourcing product development tasks; Timlon (2011) argued for a socio-economic approach in strategic outsourcing decisions; Narayanan et al. (2011) studied task complexity and end customer orientation of outsourcing decisions.

A recent study on outsourcing timing used real options methodology (Moon, 2010). Our model focuses on an investment option, mainly on the moment triggering integration, instead of an outsourcing decision. In this way, we defend the application of the model to justify irreversible costs due to own capacity investments.

The research in this paper differs from previous literature mainly in four aspects: (i) we quantify the integration decision under demand uncertainty; (ii) our model determines critical demand quantities as the moment triggering a capacity investment; (iii) we examine the impact of the uncertainties in demand for products on the trigger moment; and (iv) our model incorporates the impact of positive shocks on products’ demand, bringing it closer to reality. Although previous research might have addressed one or two of the above points, none has been found that integrates all four.

The paper makes three contributions. First, it shows that the probability of switching to the insourcing option is related with demand volatility. Second, it discusses the partial insourcing choice, and third it shows the incremental benefits of the insourcing flexibility.
MODEL FORMULATION

In this section we will begin with a description of the model before providing the optimal timing of integration.

Demand is the main source of uncertainty affecting the decisions. We assume that the demand is a stochastic variable, denoted \( D_t \), and follows a geometric Brownian motion [similar assumption in Bengtsson (2001) and Fernandes et al. (2010)], subject to a Poisson process, such that:

\[
dD_t = \mu D_t dt + \sigma D_t dz_d + D_t dq
\]

Where: 
- \( \varepsilon(t) \approx N(0,1) \)
- \( \mu = \) instantaneous drift,
- \( \sigma = \) volatility,
- \( dz = \) increment of a wiener process, where \( \varepsilon(t) \) is a serially uncorrelated and normally distributed random variable;
- \( dq = (1 + u) \) with probability \( \lambda_u \) and demand shocks intensity represented by \( u \).

It can be expected that at a certain moment there will be a demand level that supports the integration decision, considering the future outcomes. To model our problem, we will assume a different profit function prior to (outsourcing) and after the decision (full or partial integration) that we will denote as \( \pi_0 \) and \( \pi_1 \), respectively.

We consider that the integration will occur within a single period and instant production will be available to face demand changes. We assume that the decision to outsource is affected only by profit advantage, and not by competitive advantage through proper market positioning, such as the degree of product differentiation (also defended by Hamada, 2010).

The profit functions, by unit, before and after investment will be defined in the following equations, considering full integration:

\[
\begin{align*}
\pi_0(D_t) &= p_v - c_{v1}, t < t^* \\
\pi_1(D_t) &= p_v - c_{v2} - \varphi - \rho \gamma, t \geq t^*
\end{align*}
\]

With \( p_v \) representing the unit selling price, \( c_{v1} \) is the unit outsourcing cost, \( c_{v2} \) the unit integration variable cost, \( \varphi \) counts for own fixed operating costs, \( \gamma \) is the investment value, \( \rho \) discount rate, \( t^* \) is the moment when the change should occur.

The goal is the calculation of the demand critical point \( D^* \), at moment \( t^* (t^* \geq 0) \), above which the investment in integrating activities is a more profitable alternative.
Analytically we will use the following objective function:

- For full integration regime:
  \[
  \sup_{D_t} \left( \int_0^t D_t \pi_0(D_t) e^{-\rho t} dt + \int_t^{\infty} D_t \pi_1(D_t) e^{-\rho t} dt \right) \tag{3}
  \]

- For partial integration regime (\( \hat{X} \) represents the percentage of demand quantity to be produced using internal capacity):
  \[
  \sup_{D_t} \left( \int_0^t D_t \pi_0(D_t) e^{-\rho t} dt + \int_t^{\infty} \left( 1 - \hat{X} \right) D_t \pi_0(D_t) e^{-\rho t} + \hat{X} D_t \pi_1(D_t) e^{-\rho t} dt \right) \tag{4}
  \]

With:

- \( t^* \) = first optimal time to invest;
- \( \pi_0(D_t) \) = unit profit function before investment, equation;
- \( \pi_1(D_t) \) = unit profit function after investment;
- \( D_t \) = demand during time \( t \).

For the full integration regime, we will replace equations (2) with equation (3):

\[
\sup_{D_t} \left( \int_0^t e^{-\rho t} D_t (pv - cv_t) dt + \int_0^t e^{-\rho t} \left( 1 - \hat{X} \right) D_t (pv - cv_t) + \hat{X} D_t (pv - cv_t) \right) dt \tag{5}
\]

Simplifying equation (5), the objective function can be written as,

\[
\sup_{D_t} \left( \int_0^t e^{-\rho t} D_t (pv - cv_t) dt - \int_0^t e^{-\rho t} D_t (pv - cv_t) \left( 1 - \hat{X} \right) D_t (pv - cv_t) - \hat{X} D_t (pv - cv_t) \right) dt \tag{6}
\]

The first members do not depend on \( t \), so we can rewrite equation (6) as,

\[
\sup_{D_t} \left( \int_0^t e^{-\rho t} \left( \hat{X} D_t (pv - cv_t) + \hat{X} D_t (pv - cv_t) \right) dt \right) \tag{7}
\]

This equation maximizes profits from changing outsourcing to integration, under uncertain demand.

Using Oksendal (2003) theorem (also used by Pimentel, 2009), derived from Markovian property, and simplified convergence theorem, we can write equation (7) as:
As we assume that \( D_t \) follows a geometric Brownian motion subject to jumps modelled using Poisson process, the expected value at time \( t \) becomes:

\[
v(D^t) = \mathbb{E}[\mathcal{L}(D_t) | D_0 = 0] = \int_0^t e^{-\rho t} \left[ X E_{D_t}(D_t) + X E_{D_t}(D_t) - \phi - \rho \gamma \right] dt
\]

We are going to define a simple notation for each part of equation (9),

- \( Xe_{1}((p - \mu - u\lambda_u) = A \)
- \( -Xe_{2}((p - \mu - u\lambda_u) = B \)
- \( -\Phi / p = C \)
- \( -\gamma = E \)

Equation (9) can be written as,

\[
v(D^t) = A(D^t) + B(D^t) + C + E
\]

We can obtain the integration value \( v \), at the actual moment, determined by maximizing equation (10), which satisfies the following differential equation:

\[
\frac{1}{2} \sigma^2 D^2 \frac{\partial^2 v}{\partial D^2} + \mu_p D \frac{\partial v}{\partial D} - (\rho \psi + \lambda_u) v(D) + \lambda_u [1 + u] D = 0; D = D^t
\]

With:
Initial condition:
- \( v(0) = 0 \)

Value matching condition:
- \( v(D) = A.D + B.D + C + E \) with \( D = D^t \)

Smooth condition:
\[
\frac{\partial v}{\partial D} = A + B \text{ with } D = D^t
\]

If we consider (11) a second order Cauchy-Euler function (Ross, 1996), the solution can be written as:

\[
v(D) = a.D_0^5
\]
where $r_1$ is the result of the following non linear equation:

$$\frac{1}{2} \sigma^2 r_1 (r_1 - 1) + \mu r_1 - (\rho + \lambda) + \lambda_n (1 + n) = 0$$  \hspace{1cm} (13)

This can be solved numerically.

The solution of equation (11) is,

$$v(D) = e^{-r_1} \left[ A.D^{r_1} + B.D^{r_1-n} + C.D^{-n} + E.D^{r_1} \right] D^n$$  \hspace{1cm} (14)

For a given value of $D$ and for $r=0$, the value $D^*$ that maximizes $v(D)$ is given by the solution of the following equation:

$$A.D^{r_1} - B.D^{r_1-n} - C.D^{-n} - E.D^{r_1} = 0$$  \hspace{1cm} (15)

And finally, we can calculate finding the closed solution,

$$D^* = \frac{-r_1(C + E)}{(A + B)(r_1 - 1)}$$  \hspace{1cm} (16)

The flexibility source is the option to exercise. In this case, management can execute an integrating option.

**CASE ILLUSTRATION AND RESULTS**

To test our model we used data from the samples department of a flooring manufacturing company. The samples activity is intensive and depends heavily on the demand behavior, which stresses the decision of using outsourcing or integrated activities, mainly due to retailing market uncertainty. The sampling operations require one cutting machine and human tasks to be performed. The sampling process does not demand a specific workforce. The company can obtain these competences using outsourcing. Introducing the data referred in Table A1 (see p. 77) into the model, we found the following results after solving the proposed model (see Table 1. p. 70).

Considering the results computed in Table 1, the company should integrate activities when demand reaches 32.489 m$^2$. The alternative to hold the decision is valued at 439,646 euros.

First the results will be analyzed considering economic features between outsourcing and integration, more specifically, the outsourcing costs and integration investment value.
TABLE I
Integration value in pure and partial regime, considering different outsourcing costs

<table>
<thead>
<tr>
<th>Demand critical level</th>
<th>32.489</th>
<th>m³</th>
</tr>
</thead>
<tbody>
<tr>
<td>Integration option</td>
<td>439.646</td>
<td>euros</td>
</tr>
</tbody>
</table>

FIGURE 1
Integration value in pure and partial regime, considering different outsourcing costs

Figure 1 considers the costs associated with outsourcing; we find that higher outsourcing costs increase the value associated with integration, whenever internal variable costs are below the outsourcing alternative costs. In the full integration regime, the value of the opportunity is higher than in the partial alternative, which is consistent with an increase in the output of the internalized activities under a full integration. Figure 2 shows the impact of changes in investment value in both regimes. The results point to an inverse relation between integration value and investment value. The investment value is a fixed cost that is smoothed with higher internalized
activities outputs, which justifies a higher integration value for the full regime than for the partial regime.

Second, the results will be analyzed considering the intensity of the partial integration regime.

In Figure 3 (see p. 72) we compare the evolution of the integration value and the correspondent critical demand quantity. We can see that there is an inverse relation between both values. Considering only the partial regime, we simulated different scenarios for the integration percentage. As the integration percentage increases the value for the alternative between outsourcing and insourcing increases under an inverse evolution of critical demand level.

Third, the results will be analyzed considering the market demand behavior under shocks and volatility.
The results from Figure 4 (see p. 74) should be analyzed in three stages: the impact of demand volatility, the impact of demand shocks, and that impact considering different regimes for the integration decision. For the first, we conclude that in high uncertain environments there is greater potential value for integration. We can conclude that insourcing can be a flexible measure to minimize the impacts of demand uncertainty at a certain moment and under a defined critical demand level. When we consider the impact of demand shocks, we conclude that the existence of shocks intensifies the evolution of demand (we have assumed that demand follows a geometric Brownian motion) and the critical demand to support the change is anticipated, which results in lower integration value. The full integration results in a higher integration value because it is possible to use more available internal capacity. Partial integration does not allow such a fast recovery on the investment value to support the capacity investments.
FIGURE 4
Integration value and demand volatility, with and without shocks – full and partial integration regime

CONCLUSIONS AND FUTURE DEVELOPMENTS

This paper presents an optimization methodology for the integration strategy of activities where detailed aspects involving integration decision value, trigger moment and critical demand impact are considered. An optimal profit approach is then modelled, where different regimes are incorporated, considering both full and partial insourcing.

Investments in own capacity require a numerical analysis in the presence of an alternative like outsourcing. The problem raised is critical as investments to integrate became more expensive than an outsourcing option. We exposed the potential value between two alternatives using the optimal moment for the decision.
The development of the trigger moment to promote the integration of existing outsourced activities, which is based on the critical demand value, provides a relevant tool for management purposes. The incorporation of positive shocks affecting the demand evolution promotes the use of the model in realistic environments.

Our model relies on two key assumptions. First, we assume that demand conforms to geometric Brownian motion, which implies that when the demand process hits zero, it stays at zero (when the firm can go out of business). Second, we assume an infinite horizon and stable parameter values over time. Investigating the sequential change from one strategy to another by using different trigger moments, linked with demand evolution, is worthy topics for future research.

REFERENCES


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## APPENDIX

### TABLE A1
Simulation data (annual base)

<table>
<thead>
<tr>
<th>Variable</th>
<th>Value</th>
<th>Unit</th>
<th>Variable</th>
<th>Value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>$D_1$</td>
<td>$20 \times 10^3$</td>
<td>m$^2$/year</td>
<td>$\lambda_w$</td>
<td>10</td>
<td>%</td>
</tr>
<tr>
<td>$p_v$</td>
<td>20</td>
<td>Euros/m$^2$</td>
<td>$u$</td>
<td>10</td>
<td>%</td>
</tr>
<tr>
<td>$c_{v1}$</td>
<td>12</td>
<td>Euros/m$^2$</td>
<td>$\rho$</td>
<td>6</td>
<td>%/year</td>
</tr>
<tr>
<td>$c_{v2}$</td>
<td>8</td>
<td>Euros/m$^2$</td>
<td>$\mu_D$</td>
<td>3</td>
<td>%/year</td>
</tr>
<tr>
<td>$\varphi$</td>
<td>$30 \times 10^3$</td>
<td>Euros</td>
<td>$\sigma_D$</td>
<td>20</td>
<td>%</td>
</tr>
<tr>
<td>$\gamma$</td>
<td>$1 \times 10^6$</td>
<td>Euros</td>
<td>$\chi$</td>
<td>100</td>
<td>%</td>
</tr>
</tbody>
</table>